



**FIGURE 16-47** The electric field between two closely spaced parallel plates is uniform and equal to  $E = \sigma/\epsilon_0$ .

This last Example also gives us the field between the two parallel plates we discussed in Fig. 16-32d. If the plates are large compared to their separation, then the field lines are perpendicular to the plates and, except near the edges, they are parallel to each other. Therefore the electric field (see Fig. 16-47, which shows a similar very thin gaussian surface as Fig. 16-46) is also

$$E = \frac{\sigma}{\epsilon_0} = \frac{Q/A}{\epsilon_0} = \frac{Q}{\epsilon_0 A}, \quad \left[ \begin{array}{l} \text{between two closely spaced,} \\ \text{oppositely charged, parallel plates} \end{array} \right] \quad (16-10)$$

where  $Q = \sigma A$  is the charge on one of the plates.

## Summary

There are two kinds of **electric charge**, positive and negative. These designations are to be taken algebraically—that is, any charge is plus or minus so many coulombs (C), in SI units.

Electric charge is **conserved**: if a certain amount of one type of charge is produced in a process, an equal amount of the opposite type is also produced; thus the *net* charge produced is zero.

According to atomic theory, electricity originates in the atom, which consists of a positively charged nucleus surrounded by negatively charged electrons. Each electron has a charge  $-e = -1.60 \times 10^{-19}$  C.

Electric **conductors** are those materials in which many electrons are relatively free to move, whereas electric **insulators** or **nonconductors** are those in which very few electrons are free to move.

An object is negatively charged when it has an excess of electrons, and positively charged when it has less than its normal number of electrons. The net charge on any object is a whole number times  $+e$  or  $-e$ . That is, charge is **quantized**.

An object can become charged by rubbing (in which electrons are transferred from one material to another), **by conduction** (which is transfer of charge from one charged object to another by touching), or **by induction** (the separation of charge within an object because of the close approach of another charged object but without touching).

Electric charges exert a force on each other. If two charges are of opposite types, one positive and one negative, they each exert an attractive force on the other. If the two charges are the same type, each repels the other.

The magnitude of the force one point charge exerts on another is proportional to the product of their charges, and inversely proportional to the square of the distance between them:

$$F = k \frac{Q_1 Q_2}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}; \quad (16-1, 16-2)$$

this is **Coulomb's law**.

We think of an **electric field** as existing in space around any charge or group of charges. The force on another charged object is then said to be due to the electric field present at its location.

The *electric field*,  $\vec{E}$ , at any point in space due to one or more charges, is defined as the force per unit charge that would act on a tiny positive test charge  $q$  placed at that point:

$$\vec{E} = \frac{\vec{F}}{q}. \quad (16-3)$$

The magnitude of the electric field a distance  $r$  from a point charge  $Q$  is

$$E = k \frac{Q}{r^2}. \quad (16-4a)$$

The total electric field at a point in space is equal to the vector sum of the individual fields due to each contributing charge. This is the **principle of superposition**.

Electric fields are represented by **electric field lines** that start on positive charges and end on negative charges. Their direction indicates the direction the force would be on a tiny positive test charge placed at each point. The lines can be drawn so that the number per unit area is proportional to the magnitude of  $E$ .

The static electric field inside a conductor is zero, and the electric field lines just outside a charged conductor are perpendicular to its surface.

[\*In the replication of DNA, the electrostatic force plays a crucial role in selecting the proper molecules so that the genetic information is passed on accurately from generation to generation.]

[\*Photocopiers and computer printers use electric charge placed on toner particles and a drum to form an image.]

[\*The **electric flux** passing through a small area  $A$  for a uniform electric field  $\vec{E}$  is

$$\Phi_E = E_{\perp} A, \quad (16-7)$$

where  $E_{\perp}$  is the component of  $\vec{E}$  perpendicular to the surface. The flux through a surface is proportional to the number of field lines passing through it.]

[\***Gauss's law** states that the total flux summed over any closed surface (considered as made up of many small areas  $\Delta A$ ) is equal to the net charge  $Q_{\text{encl}}$  enclosed by the surface divided by  $\epsilon_0$ :

$$\sum_{\text{closed surface}} E_{\perp} \Delta A = \frac{Q_{\text{encl}}}{\epsilon_0}. \quad (16-9)$$

Gauss's law can be used to determine the electric field due to given charge distributions, but its usefulness is mainly limited to cases where the charge distribution displays much symmetry. The real importance of Gauss's law is that it is a general and elegant statement of the relation between electric charge and electric field.]